Supplement 1: Unified framework to evaluate panmixia and gene flow among multiple sampling locations using marginal likelihoods

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1 Comparison of simulated datasets: Expanded tables 2 and 3

Tables 2 and 3 in the article are abridged versions that do not highlight the strength of rejection of particular models. We present the full tables here and also give in Table 1S (Kass and Raftery 1995) the interpretation of the strength of support for the different values of the LBF. Table 2S and 3S give a more detailed answer than Table 2 and 3, but do not change the interpretation of the results. Unidirectional models models have high support even when the migration direction is incorrect when the number of parameters is small compared to the true model. Highest support among the incorrect models is given to the model with the correct migration direction and with constrained population sizes. It is not noting that this support has a clear trend in the thermodynamic integration scheme; the harmonic mean estimator does not show such a trend, but shows a high variance.

| is the Bayes factor of model 2 versus model 1 | | | | |
|---|--------------------------|--|--|--|
| $LBF_{M_2,M_1} = \log_e(BF_{M_2,M_1})$ | Evidence against Model 1 | | | |
| 0 to 1 | weak | | | |
| 1 to 3 | positive | | | |
| 3 to 5 | strong | | | |
| >5 | very strong | | | |

Table 1S: Bayes factors and strength of acceptance of a model in comparison to a reference model (?). BF_{M_2,M_1} is the Bayes factor of model 2 versus model 1

Table 2S: Comparison of the influence of the approximation on the power of LBF for simple models with different migration schemes. LBF compared a full model (Model $M_1 = [xxxx]$) with a pannictic population (Model $M_0 = [x]$). Models used to simulate the data were: (1a) a single population $(Nm \to \infty)$, the sampled individuals were split randomly into two sets; (1b) two populations exchanging many migrants (Nm = 1250); (2a) two population exchanging a moderate number of migrants (Nm = 0.25); and (2b) two populations with very low migration rate (Nm = 0.0025). The marginal likelihoods used in the LBF were approximated with thermodynamic integration (TI) with 16 and 4 temperature bins and with the harmonic mean (HM₄). The reported counts are the number of replicates that fall into the categories outlined in Table ??

| Evidence | | Counts [based on $LBF_{TI_{16}}, LBF_{TI_4}, LBF_{HM}$] | | | | | | | | | | | | |
|-------------------------|-------------|--|----------|----|--|-----|------|----|----------------|------|----|--------|--------|----|
| $(M_0: \text{ one po})$ | pulation) | | | | | | | - | | | | | | |
| | Model | | (1a) | | | | (1b) | | | (2a) | | | (2b) | |
| | Nm | | ∞ | | | - | 1250 | | | 0.25 | | (|).0025 | |
| | Method | 16 | 4 | Н | | 16 | 4 | Η | 16 | 4 | Η | 16 | 4 | Η |
| against M_0 | very strong | 0 | 1 | 0 | | 0 | 2 | 0 | 32 | 34 | 0 | 100 | 100 | 59 |
| | strong | 0 | 1 | 1 | | 0 | 2 | 0 | 10 | 6 | 1 | 0 | 0 | 3 |
| | positive | 0 | 0 | 5 | | 0 | 0 | 5 | 18 | 5 | 18 | 0 | 0 | 11 |
| | weak | 0 | 3 | 20 | | 0 | 4 | 24 | 10 | 4 | 34 | 0 | 0 | 5 |
| | Total | 0 | 5 | 26 | | 0 | 8 | 29 | 70 | 49 | 53 | 100 | 100 | 78 |
| against M_1 | weak | 1 | 1 | 40 | | 4 | 1 | 38 | 13 | 4 | 33 | 0 | 0 | 5 |
| | positive | 6 | 3 | 31 | | 4 | 3 | 30 | 10 | 3 | 13 | 0 | 0 | 2 |
| | strong | 35 | 8 | 5 | | 32 | 8 | 3 | $\overline{7}$ | 7 | 1 | 0 | 0 | 0 |
| | very strong | 57 | 82 | 0 | | 60 | 80 | 0 | 0 | 37 | 0 | 0 | 0 | 15 |
| | Total | 100 | 94 | 73 | | 100 | 92 | 71 | 30 | 51 | 47 | 0 | 0 | 22 |

Table 3S: Summary of support for specific models using LBF approximated with harmonic mean (HM) and thermodynamic integration (TI) using 16 chains with different temperatures. 100 single-locus data sets were analyzed, each with a total of 20 DNA sequences simulated using a 3-parameter model with 2 different population sizes, and unidirectional migration from population 2 to 1 (Model abbreviation is xx0x; see Methods for details). All other models 1 to 8 (M_i), such as the full model (xxxx) or the minimal model (mmmm) are compared with this 'true' model (xx0x) that represent the M_0 hypothesis. n_{param} accounts for the number of parameter estimated. Evidence

| Lindence | | | | | | | | | | | | | | | | | |
|----------------------|-----------|--|---------------------|----|---------------------------|-----|---------------------|-----|---------------------|----|---------------------|----|---------------------|-----|---------------------|----|---------------------|
| $(M_0 = xx0x)$ |) | Counts [based on LBF_{TI} and LBF_{HM}] | | | | | | | | | | | | | | | |
| n_{param} | | | 4 | | 3 | | 3 | | 3 | | 2 | | 2 | | 2 | | 1 |
| Model | | XX | XX | x | $0 \mathbf{x} \mathbf{x}$ | xm | mx | mx | xm | m | x0m | m | Oxm | mm | mm | | x |
| Approximat | ion | ΤI | HM | ΤI | HM | ΤI | HM | ΤI | HM | ΤI | HM | ΤI | HM | ΤI | HM | ΤI | HM |
| against M_0 | very str. | 0 | 1 | 0 | 0 | 0 | 3 | 0 | 4 | 0 | 1 | 0 | 1 | 0 | 1 | 9 | 10 |
| | strong | 0 | 4 | 1 | 2 | 0 | 1 | 0 | 1 | 0 | 4 | 0 | 3 | 0 | 6 | 0 | 1 |
| | positive | 0 | 22 | 3 | 13 | 0 | 23 | 0 | 27 | 20 | 21 | 17 | 17 | 0 | 28 | 0 | 16 |
| | weak | 0 | 19 | 24 | 21 | 0 | 21 | 0 | 25 | 50 | 24 | 37 | 14 | 0 | 24 | 2 | 13 |
| | | 0 | 46 | 28 | 36 | 0 | 48 | 0 | 57 | 70 | 50 | 54 | 35 | 0 | 59 | 11 | 40 |
| against M_i | weak | 0 | 26 | 38 | 18 | 0 | 24 | 0 | 17 | 22 | 16 | 24 | 24 | 0 | 19 | 0 | 19 |
| | positive | 2 | 21 | 31 | 31 | 2 | 21 | 1 | 23 | 7 | 25 | 20 | 26 | 1 | 18 | 18 | 23 |
| | strong | 66 | 5 | 3 | 6 | 63 | 4 | 46 | 3 | 0 | 5 | 1 | 10 | 44 | 3 | 18 | 4 |
| | very str. | 32 | 2 | 0 | 9 | 35 | 3 | 53 | 0 | 1 | 4 | 1 | 5 | 55 | 1 | 53 | 14 |
| | | 100 | 54 | 72 | 64 | 100 | 52 | 100 | 43 | 30 | 50 | 46 | 65 | 100 | 41 | 89 | 60 |
| Different da | ta sets | 76 | 76 | 97 | 97 | 89 | 89 | 88 | 88 | 99 | 99 | 99 | 99 | 98 | 98 | 96 | 96 |

2 Run conditions for Figure 1

Ten artificial two-population data sets were created with the programs migtree and migdata using the following settings:

| Mutation model | F84-model with | h transition/transversion ratio=2.0 | | | |
|-----------------------------|--------------------|-------------------------------------|--|--|--|
| Mutation rate | 2×10^{-6} | | | | |
| Sequence length | 1000 | | | | |
| Population model | Population 1 | Population 2 | | | |
| Population size $N_e^{(i)}$ | 625 | 1250 | | | |
| Immigration rate m_{ji} | 0.0002 | 0.0 | | | |
| Sample size | 10 | 10 | | | |

Each data set was run under 3 different heating schemes with the following temperature settings:

| Chains | Temperature settings $T_i = 1/t_i$. Ordering is T_1T_n |
|--------|---|
| 4 | 1.0, 1.5, 3.0, 1000000.0 |
| 16 | 1.0, 1.071, 1.154, 1.25, 1.364, 1.5, 1.667, 1.875, 2.143, 2.5, 3.0, 3.75, 5.0, 7.5, |
| | 15.0, 1000000.0 |
| 32 | 1.0, 1.03, 1.069, 1.107, 1.148, 1.19, 1.24, 1.29, 1.35, 1.41, 1.48, 1.55, 1.63, 1.72, |
| | 1.82, 1.94, 2.07, 2.21, 2.38, 2.58, 2.82, 3.10, 3.44, 3.875, 4.429, 5.167, 6.2, 7.75, |
| | 10.33, 15.5, 31.0, 1000000.0 |

All other settings were at the default values except the following:

| Increment (sampling every x state) | 1,000 |
|------------------------------------|-----------------|
| Sampled states | 20,000 |
| Discarded states | $1,\!000,\!000$ |

3 Run conditions for Figure 3

One random dataset from the artificial data sets used in Figure 1 was used. Same temperatures as for Figure 1, but run parameters where changed to

| Relative run-length | Increment (sampling every x state) | Sampled states | Discarded states |
|---------------------|------------------------------------|----------------|------------------|
| 1 | 100 | 200 | 10,000 |
| 2 | 100 | 400 | 20,000 |
| 4 | 100 | 800 | 40,000 |
| 8 | 100 | 1,600 | 80,000 |
| 16 | 100 | 3,200 | 160,000 |
| 32 | 100 | 6,400 | 320,000 |
| 64 | 100 | 12,800 | 640,000 |
| 128 | 100 | 25,600 | 1,280,000 |
| 256 | 100 | 51,200 | 2,560,000 |

4 Run conditions for Figure 4

Run conditions were identical to figure 1.

5 Run conditions for Table 2

100 artificial data sets for the Model xx0x were generated:

| Population model | Parameters | Population 1 | Population 2 |
|------------------|-----------------------------|--------------------|--------------|
| Two populations | Population size $N_e^{(i)}$ | 625 | 1250 |
| (Model xx0x) | mutation rate | 2×10^{-6} | |
| | Immigration rate m_{ji} | 0.0002 | 0.0 |
| | Sample size | 10 | 10 |

The mutation model was F84 with a mutation rate of 0.000002. Each sequence was 1000 base pairs long. All run parameters were identical to Figure 1, but the runs used different population models as indicated in Table 2. The runs were executed on the High-performance cluster at Florida State University using the commonly available backfill queue. This queue allows runs maximally 4 hours long, which resulted in some table cells with fewer than 100 runs. A total of 900 runs were executed for Table 2.

6 Run conditions for Table 3

| Population model | Parameters | Population 1 | Population 2 |
|-------------------|-----------------------------|--------------------|--------------------|
| Single population | Population size $N_e^{(i)}$ | 1250 | - |
| (Model 1a) | Mutation rate | 2×10^{-6} | |
| | Immigration rate m_{ji} | - | - |
| | Sample size | 20 | |
| Two populations | Population size $N_e^{(i)}$ | 625 | 625 |
| (Model 1b) | Mutation rate | 2×10^{-6} | 2×10^{-6} |
| | Immigration rate m_{ji} | 1.0 | 1.0 |
| | Sample size | 10 | 10 |
| Two populations | Population size $N_e^{(i)}$ | 625 | 625 |
| (Model 2a) | Mutation rate | 2×10^{-6} | 2×10^{-6} |
| | Immigration rate m_{ji} | 0.0002 | 0.0002 |
| | Sample size | 10 | 10 |
| Two populations | Population size $N_e^{(i)}$ | 625 | 625 |
| $(Model \ 2b)$ | Mutation rate | 2×10^{-6} | 2×10^{-6} |
| | Immigration rate m_{ji} | 0.000002 | 0.000002 |
| | Sample size | 10 | 10 |

100 artificial data sets for each of the following population models were generated:

The mutation model was F84 with a mutation rate of 0.000002. Each sequence was 1000 base pairs long. All run parameters were identical to Figure 1. Each data set was run twice for each of the approximation methods (TI_4 , TI_{16}), with the single population model x and with the unrestricted two-population model xxxx.

7 Run conditions for Table 4: Effect of number of loci on Bayes factors

| All parameter settings were default, except | | | | | |
|--|--|--|--|--|--|
| Prior distribution for mutation-scaled population size | Uniform with range 0.0 to 0.1 | | | | |
| Prior distribution for mutation-scaled migration rates | Uniform with range 0.0 to 1000 | | | | |
| Increment between samples | 100 | | | | |
| Samples per replicate | 1,000 | | | | |
| Burn-ins per replicate | 100,000 | | | | |
| Replicates | 10 | | | | |
| Heating | static with temperatures 1, 1.5, 3, 10^6 | | | | |

8 Run conditions for Table 5: Effect of prior distribution on Bayes factors

| All parameter settings were default, except | | | | | |
|---|---------------------------------|---------------------------------|--|--|--|
| Type | Priors for | | | | |
| | Mutation-scaled population size | Mutation-scaled migration rates | | | |
| | Minimum - Mean - Maximum | Minimum - Mean - Maximum | | | |
| Uniform narrow | 0-0.05-0.1 | 0.0 - 2500 - 5000 | | | |
| Uniform wide | 0-0.25 -0.1 | $0.0 - 25,\!000 - 50,\!000$ | | | |
| Exponential narrow | $0 \ -0.01 \ - \ 0.1$ | $0.0 - 100 - 5{,}000$ | | | |
| Exponential wide | $0-0.1\!\!-0.5$ | $0.0 - 2,\!000 - 50,\!000$ | | | |

9 Run conditions for Table 6: Humpback whale example

| Mutation model | F84-model |
|--|-----------------------------------|
| Transition/transversion ratio | 11.400000 |
| Site rate modifier (3 groups) | $0.416751 \ 2.274676 \ 6.216591$ |
| Probabilities of site rates | $0.708460 \ 0.280989 \ 0.010551$ |
| Prior distribution for mutation-scaled population size | Uniform with range 0.0 to 0.1 |
| Prior distribution for mutation-scaled migration rates | Uniform with range 0.0 to 5000 |
| Increment between samples | 200 |
| Samples per replicate | 5,000 |
| Burn-ins per replicate | 100,000 |
| Replicates | 50 |

Proposal distribution for parameters was Slice-sampling, whereas the genealogy proposals were using Metropolis-Hastings.